

## Sistemas mecanicamente isolados

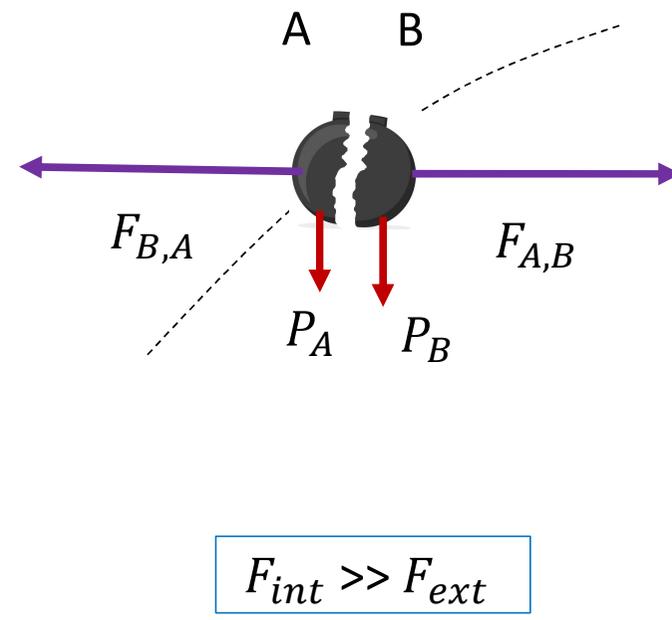
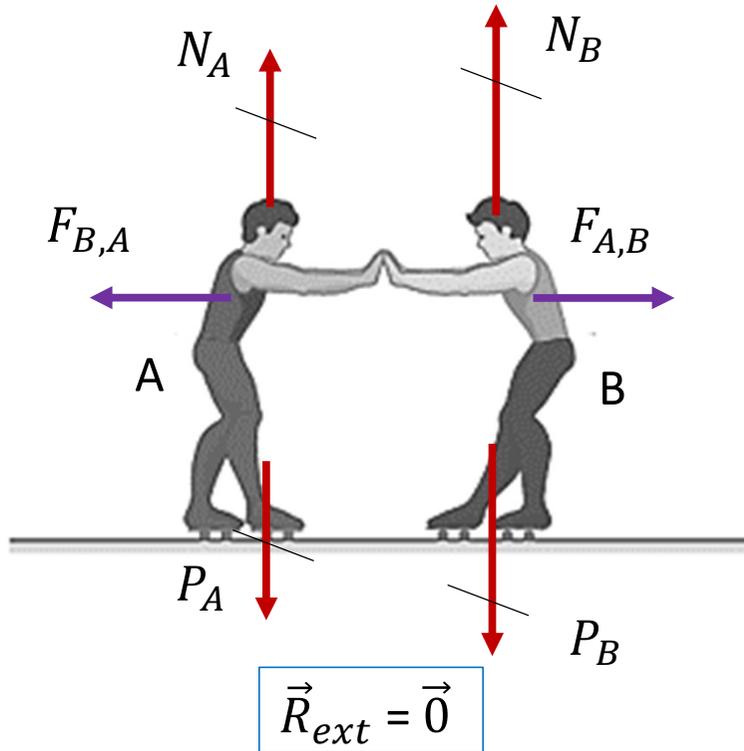
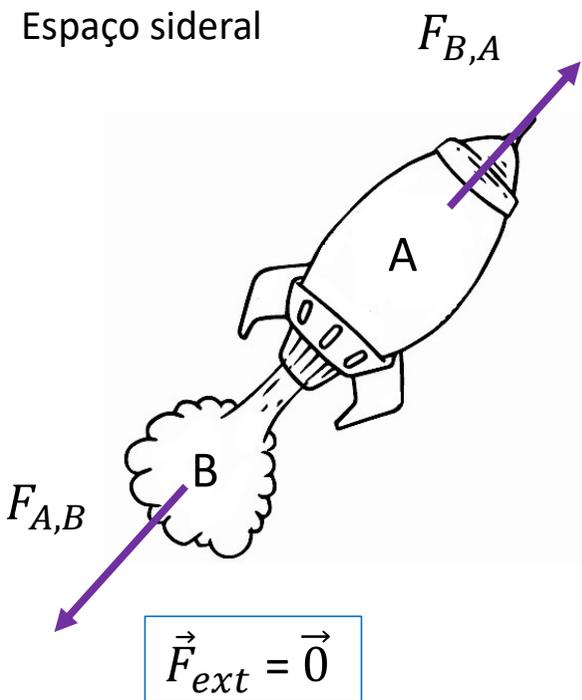
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**Professor Caio – Física / Setor A**

# 1. Sistemas mecanicamente isolados (de forças externas)

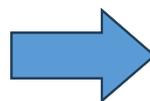
Espaço sideral



$$\vec{I}_{sistema} = \vec{I}_{ext} + \vec{I}_{int} = \Delta \vec{Q}_{sistema}$$

$\vec{I}_{ext} = 0$        $\vec{I}_{int} = 0$  (sempre)

$$\Delta \vec{Q}_{sistema} = \vec{0}$$



$$\vec{Q}'_{sistema} = \vec{Q}_{sistema}$$

$$\vec{Q}'_A + \vec{Q}'_B = \vec{Q}_A + \vec{Q}_B$$

## Exemplos

$$\vec{I}_{sistema} = \vec{I}_{ext} + \vec{I}_{int} = \Delta \vec{Q}_{sistema}$$

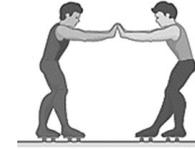
$\nearrow 0$        $\nearrow 0$  (sempre)

Sistemas  
mecanicamente  
isolados

$$\Delta \vec{Q}_{sistema} = \vec{0}$$

$$\vec{Q}'_{sistema} = \vec{Q}_{sistema}$$

- Patinadores



$$\vec{R}_{ext} = \vec{0}$$

- Colisões



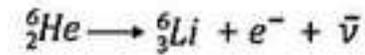
$$F_{int} \gg F_{ext}$$

- Explosões



$$F_{int} \gg F_{ext}$$

- Decaimentos



$$F_{int} \gg F_{ext}$$

- Disparos



$$F_{int} \gg F_{ext}$$

- Espaço sideral

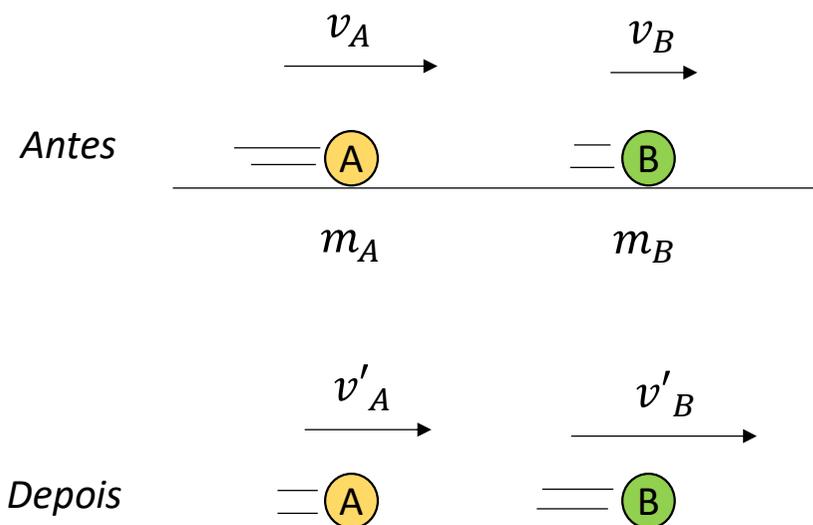


$$\vec{F}_{ext} = \vec{0}$$

## Casos unidimensionais



Fazer o tratamento algébrico



### Sistema mecanicamente isolado

$$\vec{Q}'_{sistema} = \vec{Q}_{sistema}$$

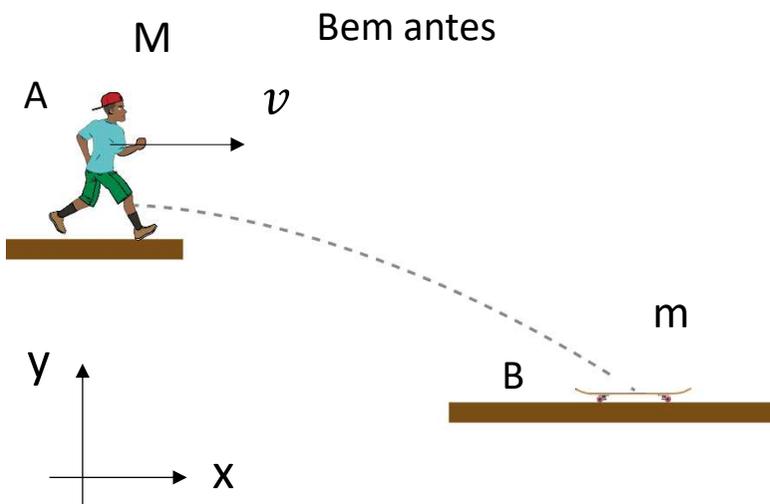
$$\vec{Q}'_A + \vec{Q}'_B = \vec{Q}_A + \vec{Q}_B$$

$$Q'_A + Q'_B = Q_A + Q_B$$

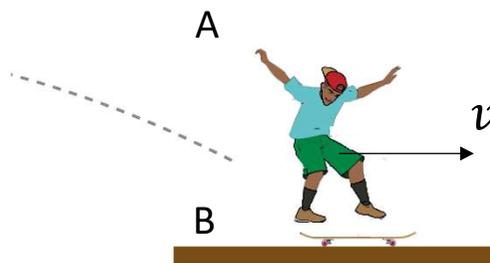
$$m_A \cdot v'_A + m_B \cdot v'_B = m_A \cdot v_A + m_B \cdot v_B$$

→ (+)

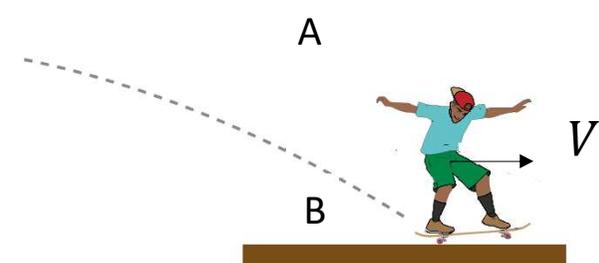
## 2. Sistemas mecanicamente isolados em uma única direção



Imediatamente antes



Imediatamente depois



**Eixo y**

Existem forças externas não equilibradas

**Eixo x:**

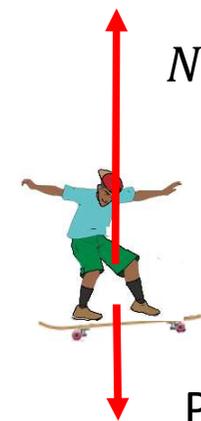
$$\vec{F}_{ext} = \vec{0}$$

$$\vec{R}_{ext} = \vec{0}$$

$$F_{int} \gg F_{ext}$$

$$Q'_{sist}(x) = Q_{sist}(x)$$

$$(m + M).V' = 0 + M.v$$



### 3. Sistemas mecanicamente isolados e sistemas conservativos

Sistema	Causa	Consequência
Isolado	$\vec{F}_{ext} = \vec{0}$ ou $\vec{R}_{ext} = \vec{0}$ ou $F_{int} \gg F_{ext}$	$\vec{Q}_{sist.} = \vec{Q}'_{sist.}$
Conservativo	$\tau = 0$ Forças não conservativas	$E_m = E'_m$

## Colisões frontais

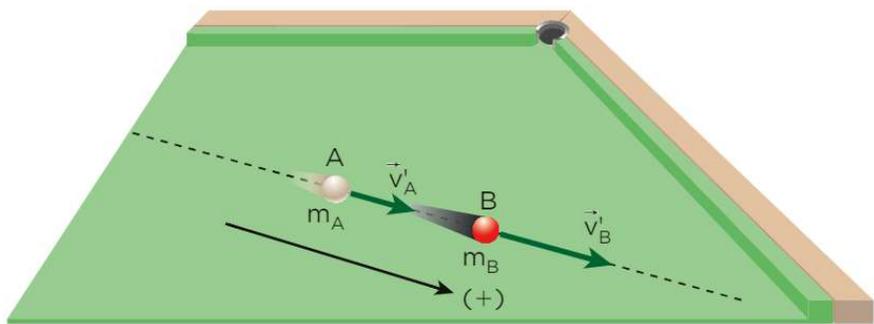
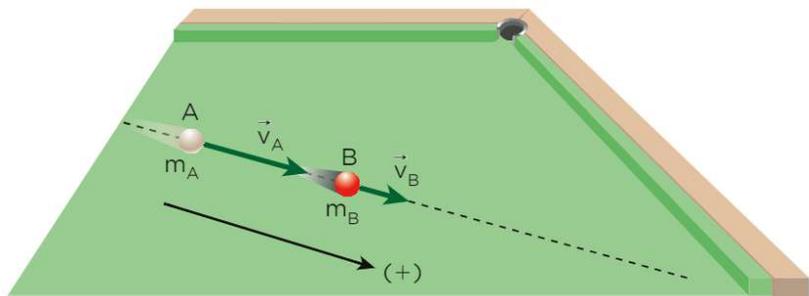
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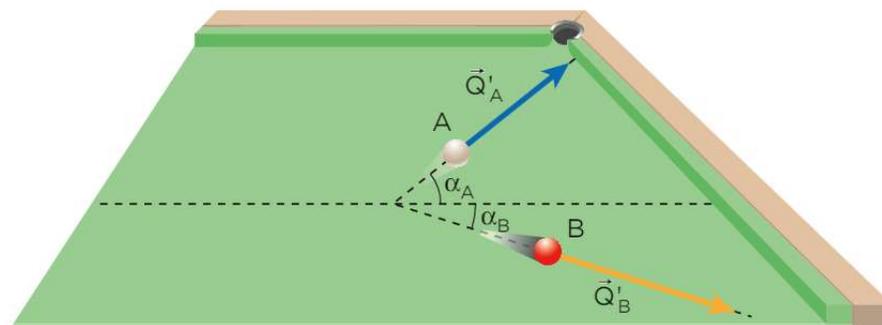
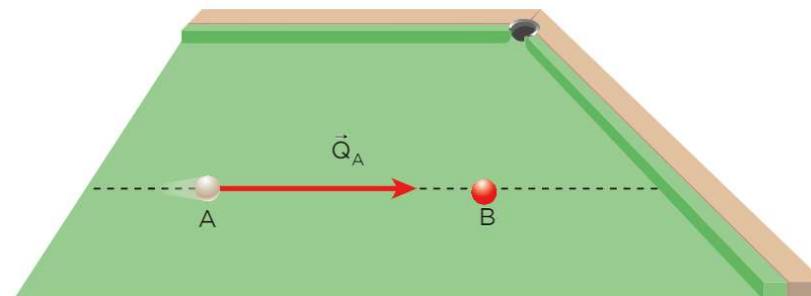
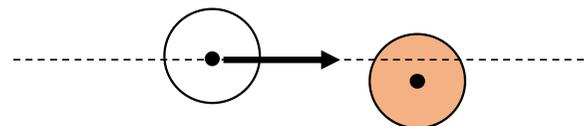
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# 1. Colisão frontal

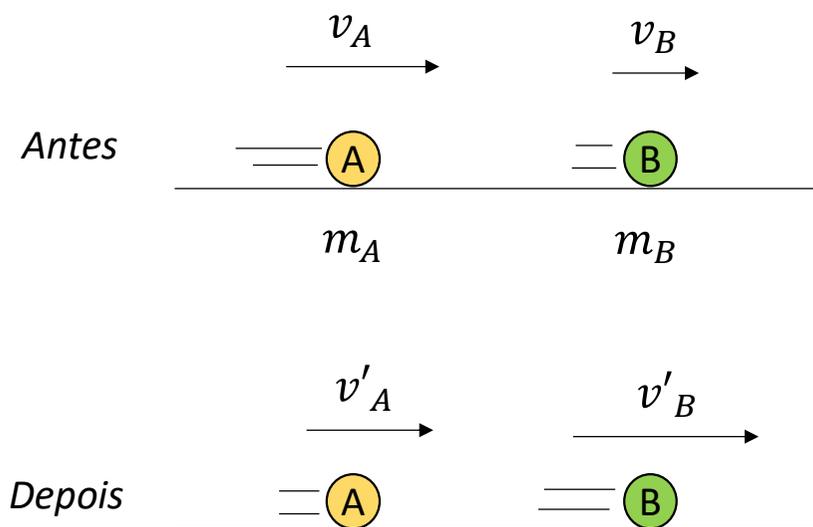
## Colisão frontal



## Colisão oblíqua



## Colisão frontal



Sistema mecanicamente isolado

$$Q'_A + Q'_B = Q_A + Q_B$$

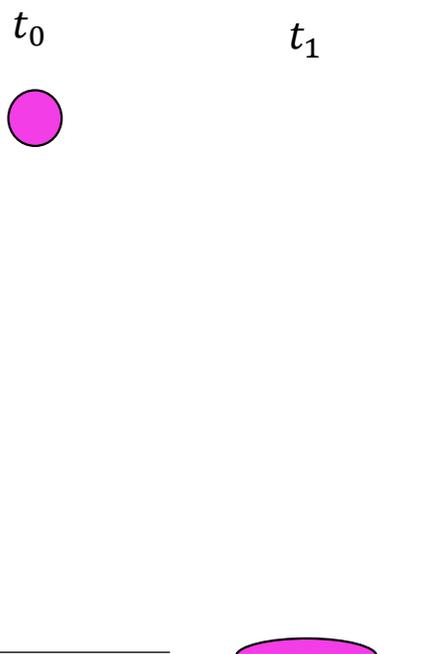
$$m_A \cdot v'_A + m_B \cdot v'_B = m_A \cdot v_A + m_B \cdot v_B$$

Coefficiente de restituição (e)

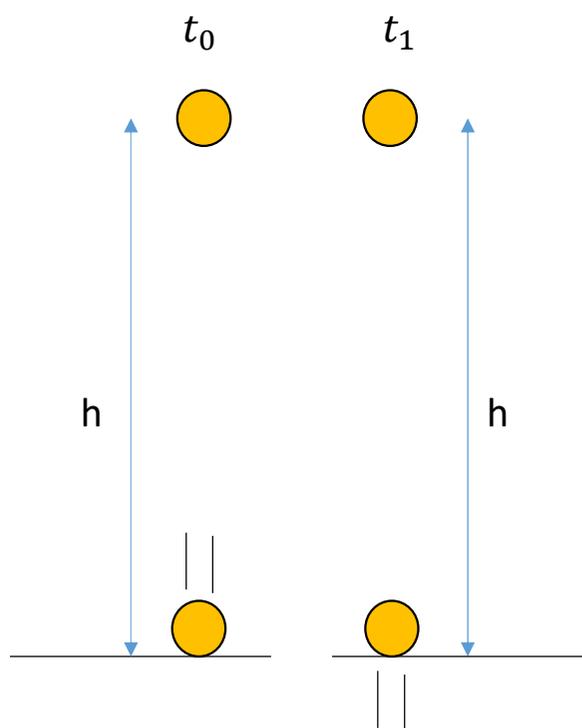
$$e = \frac{v_{afastamento}}{v_{aproximação}} = \frac{v_{B'} - v_{A'}}{v_A - v_B}$$

- $e = 1$  → perfeitamente elástica / elástica → sem perda de  $E_c$  →  $E_{c(f)} = E_{c(i)}$
- $0 < e < 1$  → parcialmente elástica
- $e = 0$  → inelástica / anelástica / plástica → máxima perda  $E_{cinética}$  (corpos grudados no final)

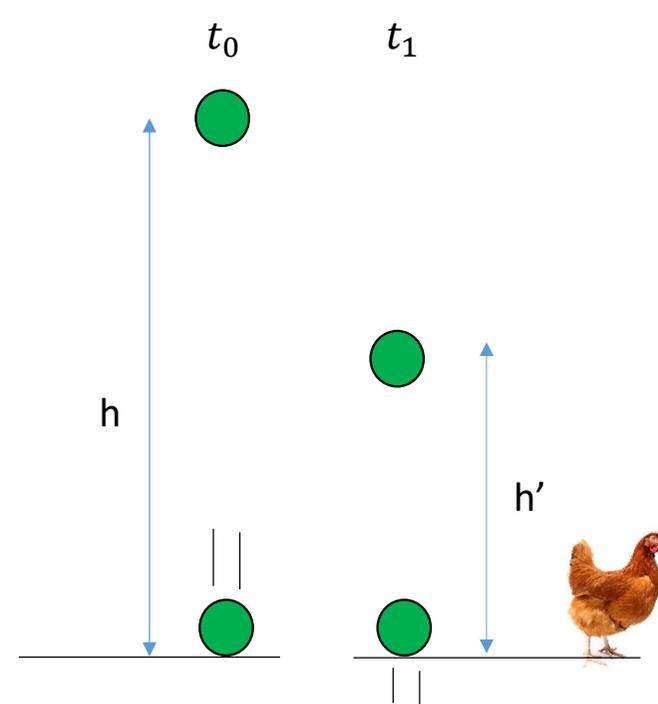
## Colisão contra o chão ou uma parede



$$e = \frac{v_{afastamento}}{v_{aproximação}} = 0$$



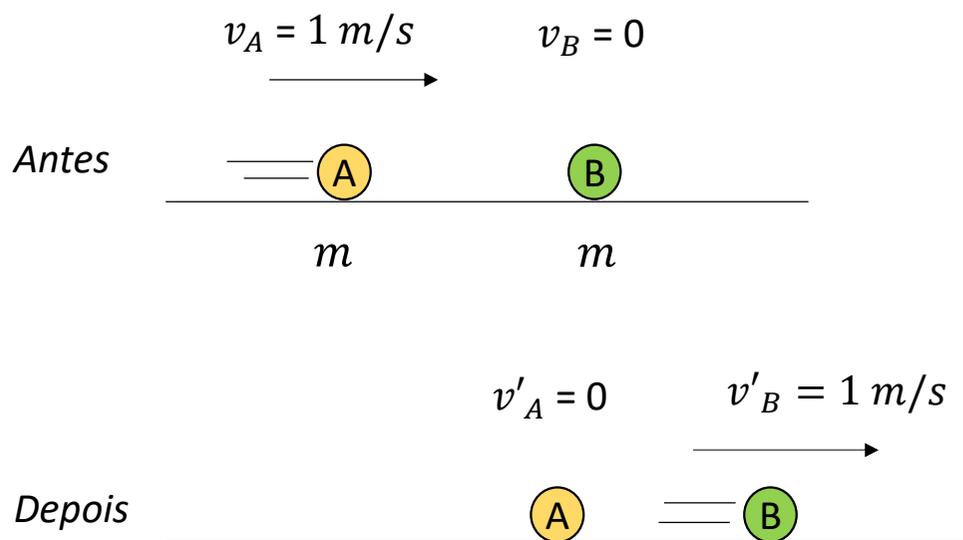
$$e = \frac{v_{afastamento}}{v_{aproximação}} = 1$$



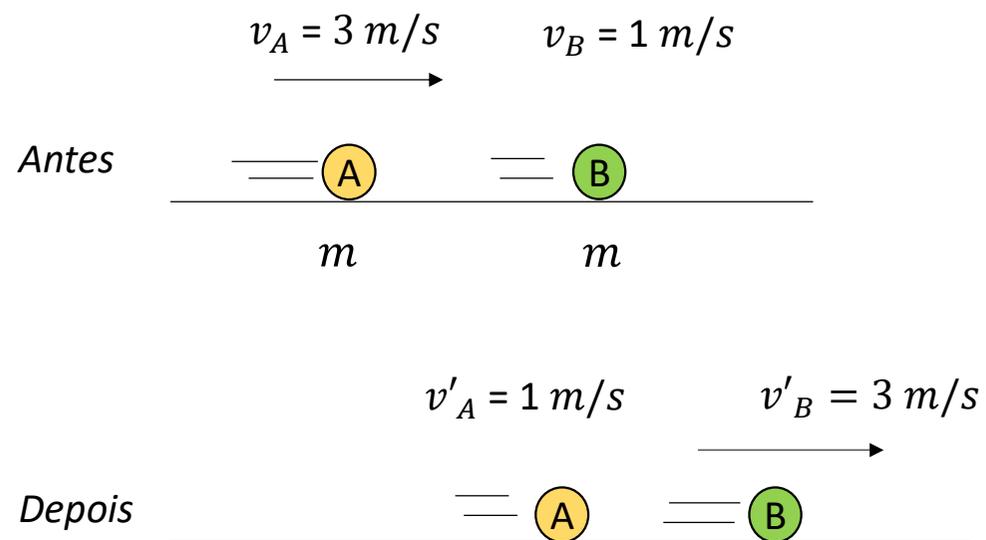
$$e = \frac{v_{afastamento}}{v_{aproximação}} = 0,5$$

## Caso particular: colisão perfeitamente elástica entre corpos de mesma massa

Exemplo 1



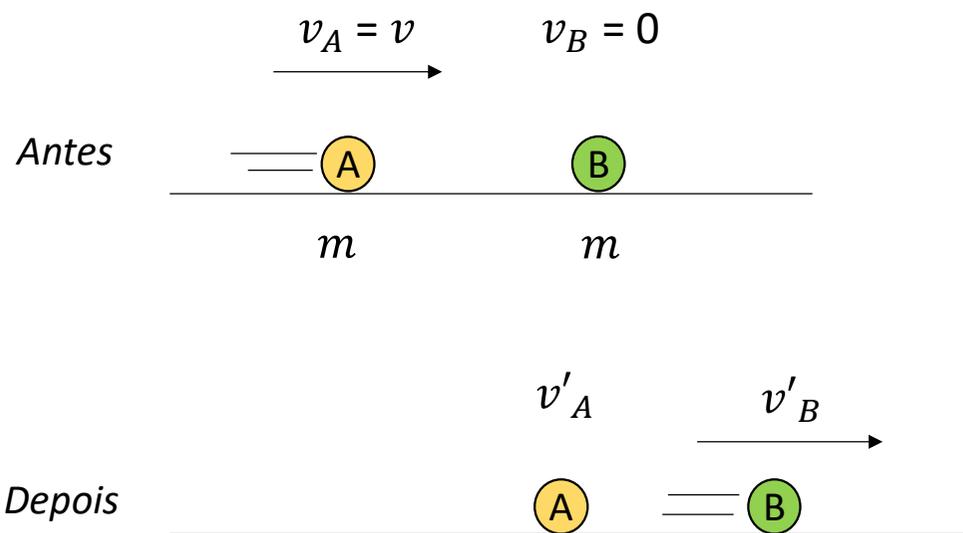
Exemplo 2



Permuta de velocidades



## Caso particular: colisão perfeitamente elástica entre corpos de mesma massa



$$m_A \cdot v'_A + m_B \cdot v'_B = m_A \cdot v_A + m_B \cdot v_B$$

$$\cancel{m} \cdot v'_A + \cancel{m} \cdot v'_B = \cancel{m} \cdot v + \cancel{m} \cdot 0$$

$$v'_A + v'_B = v$$

$$e = \frac{v_{\text{afastamento}}}{v_{\text{aproximação}}} = \frac{v_B' - v_A'}{v_A - v_B}$$

$$1 = \frac{v_B' - v_A'}{v - 0}$$

$$v_B' - v_A' = v$$

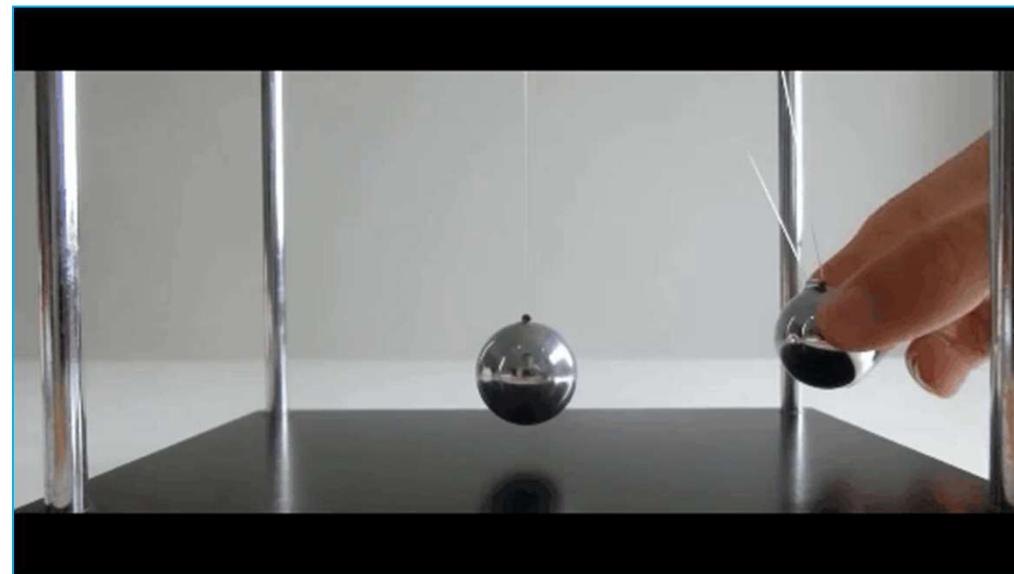
$$+ \begin{cases} v'_A + v'_B = v \\ v'_B - v'_A = v \end{cases}$$

$$2v'_B = 2v$$

$$v'_B = v$$

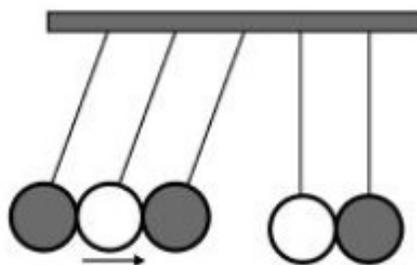
$$v'_A = 0$$

Caso particular: colisão perfeitamente elástica entre corpos de mesma massa

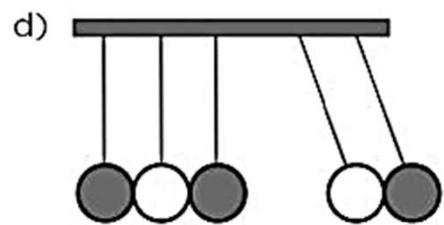
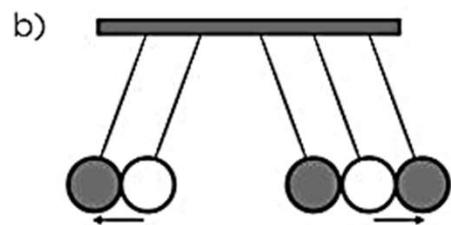
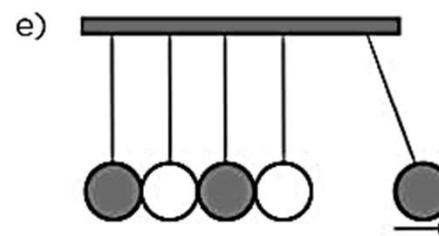
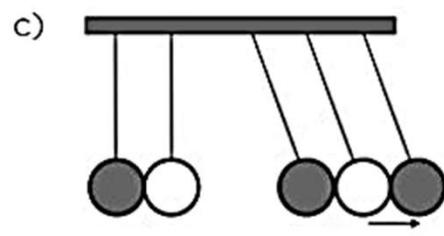
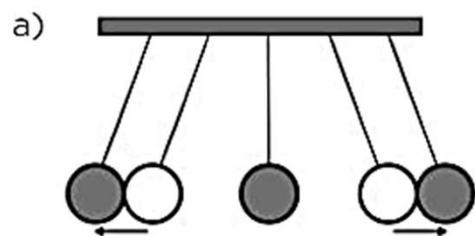


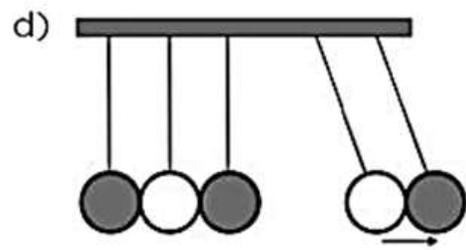
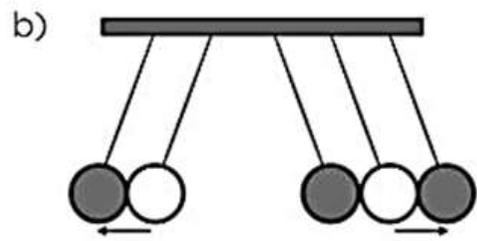
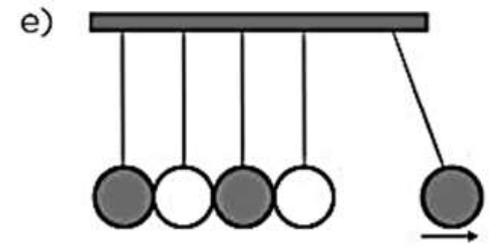
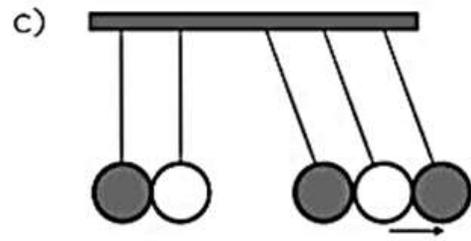
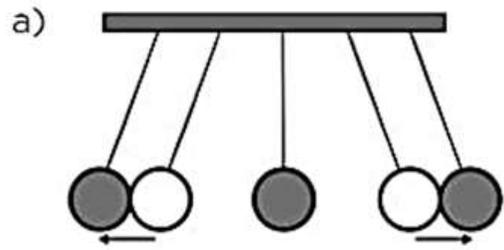
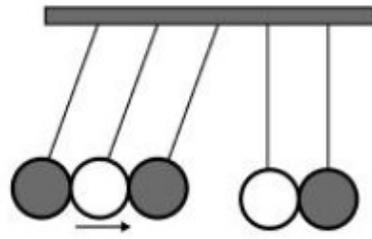
# Exercícios

8. (Enem) O pêndulo de Newton pode ser constituído por cinco pêndulos idênticos suspensos em um mesmo suporte. Em um dado instante, as esferas de três pêndulos são deslocadas para a esquerda e liberadas, deslocando-se para a direita e colidindo elasticamente com as outras duas esferas, que inicialmente estavam paradas.

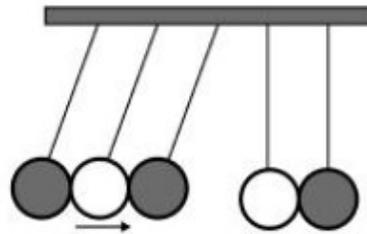


O movimento dos pêndulos após a primeira colisão está representado em:



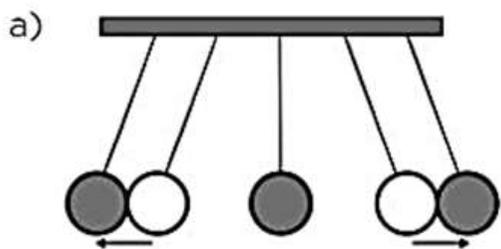


$$Q_{\text{antes}} = 3mv$$



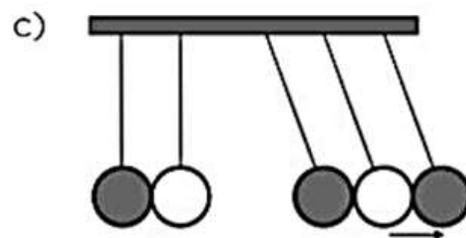
+

✗



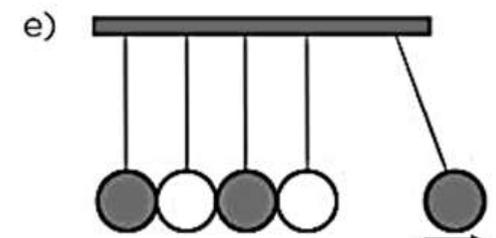
$$Q_{\text{depois}} = -2mv + 2mv = 0$$

✓



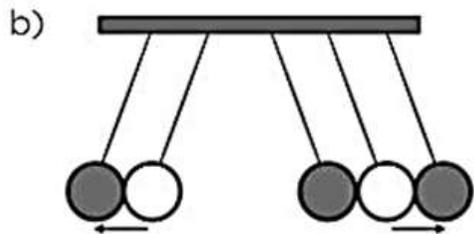
$$Q_{\text{depois}} = 3mv$$

✗



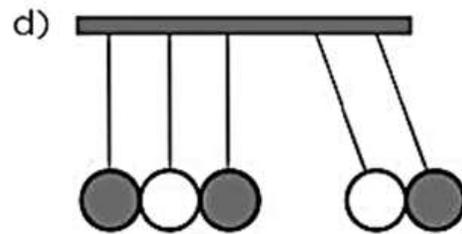
$$Q_{\text{depois}} = mv$$

✗



$$Q_{\text{depois}} = -2mv + 3mv = mv$$

✗



$$Q_{\text{depois}} = 2mv$$